

PHYSICAL CONSTANTS

Speed of Light $c = 3 \times 10^8 \text{ m/s}$

Planck constant $h = 6.63 \times 10^{-34} \text{ Js}$ $hc = 1242 \text{ eV-nm}$

Gravitation constant $G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$

Boltzmann constant $k = 1.38 \times 10^{-23} \text{ J/K}$

Molar gas constant $R = 8.314 \text{ J/mol.K}$

Avogadro's number $N_A = 6.023 \times 10^{23} / \text{mol}$

Charge of electron $e = 1.602 \times 10^{-19} \text{ C}$

Permeability of vacuum $\mu_0 = 4\pi \times 10^{-7} \text{ N/A}^2$

Permittivity of vacuum $\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$

Coulomb constant $1/4\pi\epsilon_0 = 9 \times 10^9 \text{ Nm}^2/\text{C}^2$

Faraday constant $F = 96485 \text{ C/mol}$

Mass of electron $m_e = 9.1 \times 10^{-31} \text{ kg}$

Mass of proton $m_p = 1.6726 \times 10^{-27} \text{ kg}$

Mass of neutron $m_n = 1.6749 \times 10^{-27} \text{ kg}$

Atomic mass unit $u = 1.66 \times 10^{-27} \text{ kg}$

Stefan-Boltzmann constant $\sigma = 5.67 \times 10^{-8} \text{ W/m}^2\text{K}^4$

Rydberg constant $R_\infty = 1.097 \times 10^7 / \text{m}$

Bohr magneton $\mu_B = 9.27 \times 10^{-24} \text{ J/T}$

Bohr radius $a_0 = 0.529 \times 10^{-10} \text{ m}$

Standard atmosphere $\text{atm} = 1.01325 \times 10^5 \text{ Pa}$

Wien displacement constant $b = 2.9 \times 10^{-3} \text{ mK}$

VECTORS

$$\vec{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k} \quad |\vec{a}| = \sqrt{a_x^2 + a_y^2 + a_z^2}$$

DOT PRODUCT $\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z$
 $= ab \cos \theta$

CROSS PRODUCT $\vec{a} \times \vec{b} = ab \sin \theta$

$$\vec{a} \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix} = (a_y b_z - b_y a_z) \hat{i} + (a_z b_x - b_z a_x) \hat{j} + (a_x b_y - b_x a_y) \hat{k}$$

KINEMATICS

$$\vec{v}_{\text{avg}} = \Delta \vec{s} / \Delta t \quad \vec{v}_{\text{inst}} = d\vec{s} / dt$$

$$\vec{a}_{\text{avg}} = \Delta \vec{v} / \Delta t \quad \vec{a}_{\text{inst}} = d\vec{v} / dt$$

$$s = ut + \frac{1}{2} at^2$$

$$v = u + at$$

$$v^2 = u^2 + 2as$$

RELATIVE VELOCITY

$$\vec{v}_{A/B} = \vec{v}_A - \vec{v}_B$$

PROJECTILE MOTION

$$u_x = u \cos \theta$$

$$u_y = u \sin \theta$$

$$H = u^2 \sin^2 \theta / 2g$$

Time of Flight $= 2u_y / g \Rightarrow T = 2u \sin \theta / g$

Range $= u_x \cdot T \Rightarrow R = u^2 \sin 2\theta / g$

$$y = \tan \theta \cdot x - \left(\frac{g}{2u^2 \cos^2 \theta} \right) \cdot x^2$$

LAWS OF MOTION

1st LAW: INERTIA 2nd LAW: $F = d\vec{p} / dt = m\vec{a}$ 3rd LAW: Action $\Rightarrow$ Reaction

Friction: $f_{\text{static, maximum}} = \mu_s N$ $f_{\text{kinetic}} = \mu_k N$

Centripetal force $= \frac{mv^2}{r} = m\omega^2 r$



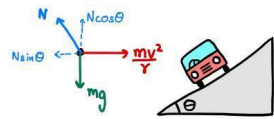
$$T \sin \theta = mv^2 / r$$

$$T \cos \theta = mg$$

$$\tan \theta = v^2 / rg$$

minimum speed for VERTICAL CIRCULAR MOTION

$$\sqrt{5gl}$$



CURVED BANKING

$$\frac{v^2}{rg} = \tan \theta \quad \frac{v^2}{rg} = \frac{\mu + \tan \theta}{1 \mp \mu \tan \theta}$$

WORK, POWER & ENERGY

Work $= \vec{F} \cdot \vec{s} = Fs \cos \theta$

$$= \int \vec{F} \cdot d\vec{s}$$

KE $= \frac{1}{2} mv^2$

POTENTIAL ENERGY (U)

$U_g = mgh$ $\vec{F} = -\frac{dU}{dx}$

$U_{\text{spring}} = \frac{1}{2} kx^2$

K + U = Conserved

$\oint \vec{F} \cdot d\vec{s} = 0$ {work by Conservative force in a closed path}

WORK-ENERGY THEOREM

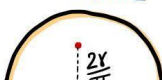
$$W_{\text{net}} = \Delta K$$

POWER $= dW / dt = \vec{F} \cdot \vec{v}$

CENTER OF MASS

$$x_{\text{cm}} = \frac{\sum x_i m_i}{\sum m_i} = \frac{\int x dm}{\int dm}$$

$$\vec{v}_{\text{cm}} = \frac{\sum m_i \vec{v}_i}{\sum m_i} \quad \vec{F} = m \vec{a}_{\text{cm}}$$



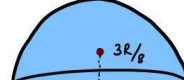
HOLLOW CONE $= h/3$



SOLID CONE $= h/4$



HOLLOW $= R/2$



SOLID $= 3R/8$

COLLISION

$$\frac{m_1}{u_1} \rightarrow \frac{m_2}{u_2} \quad \frac{m_1}{v_1} \rightarrow \frac{m_2}{v_2}$$

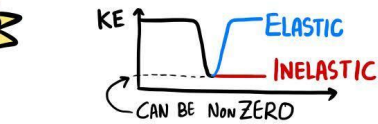
MOMENTUM CONSERVATION {Always}

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$

$m_1 \gg m_2$

$m_1 \rightarrow$ undisturbed motion

Solve using CoR in m_1 Frame



CoR $= e = \frac{V_{\text{SEPARATION}}}{V_{\text{APPROACH}}} = \frac{v_2 - v_1}{u_1 - u_2}$

ENERGY CONSERVATION {Elastic}

$$\frac{1}{2} m_1 u_1^2 + \frac{1}{2} m_2 u_2^2 = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2$$

RIGID BODY DYNAMICS

$$\omega = \frac{\Delta \theta}{\Delta t} = \frac{d\theta}{dt} \quad \alpha = \frac{\Delta \omega}{\Delta t} = \frac{d\omega}{dt} \quad \vec{v} = \vec{\omega} \times \vec{r} \quad \vec{a}_{\text{tan}} = \vec{\alpha} \times \vec{r} \quad \vec{a}_{\text{centri}} = \omega^2 r$$

$$\theta = \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\omega = \omega_0 + \alpha t$$

$$\omega^2 = \omega_0^2 + 2\alpha \theta$$

$$\vec{L} = \vec{r} \times \vec{p} = m\vec{r} \times \vec{v}$$

$$\vec{\tau} = I\vec{\alpha} = d\vec{L} / dt$$

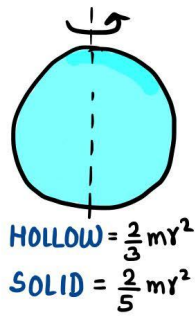
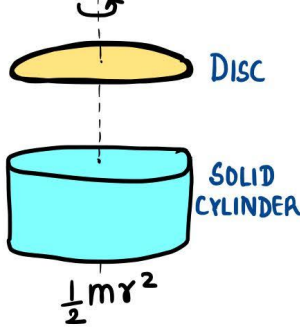
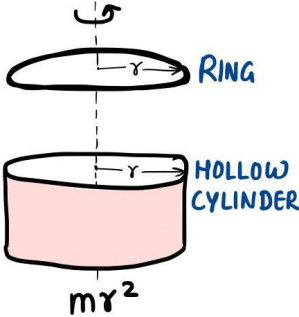
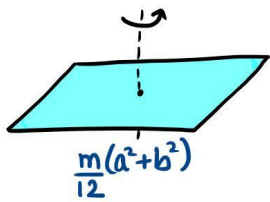
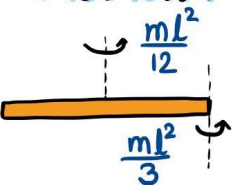
$$\vec{\tau} = \vec{r} \times \vec{F} = r_{\perp} F = r F \sin \theta$$

EQUILIBRIUM: $F_{\text{net}} = 0 = \tau_{\text{net}}$

$\omega = 2\pi f$ $T = 1/f$

$\omega = v_{\perp} / r$

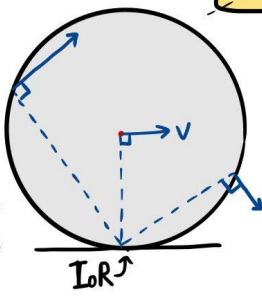
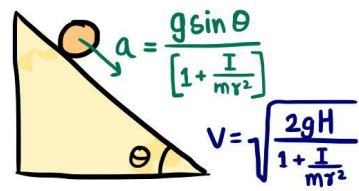
MOMENT OF INERTIA



$I = \sum m_i r_i^2$
 $I = \int r^2 dm$
 $R_{GYRATION} \quad mk^2 = I$

KINETIC ENERGY

$K = \frac{1}{2}mv_c^2 + \frac{1}{2}I_c\omega^2$
 $K = \frac{1}{2}I_H\omega^2 \text{ \{About Hinge\}}$
 or I_{OR}

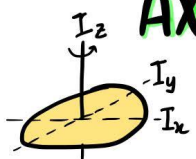


ROLLING MOTION

$v = \omega R$ (no slip condition)

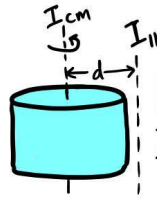
I_{OR} INSTANTANEOUS AXIS OF ROTATION
 $\vec{v} = \vec{\omega} \times \vec{r}$

AXIS THEOREMS



PERPENDICULAR

$I_z = I_x + I_y$



PARALLEL

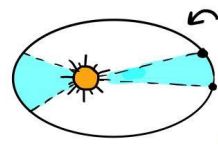
$I_{||} = I_{cm} + md^2$

GRAVITATION

$F = G \frac{Mm}{R^2}$ POT. ENERGY $(U) = -GMm/R$
 $g = G \frac{M}{R^2}$ $g' = g[1 - \frac{d}{R_e}]$ $g' \approx g[1 - \frac{2h}{R_e}]$



$g' = g - \omega^2 R \cos^2 \theta$



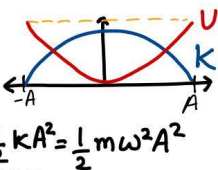
KEPLER'S LAWS

- 1st Elliptical Orbits, Sun @ foci
- 2nd Equal Area in Equal time ($\vec{L}$)
- 3rd $T^2 \propto a^3$ [semi major axis]

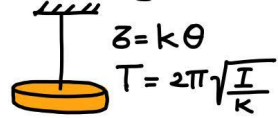
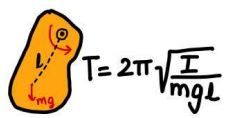
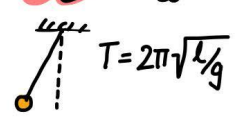
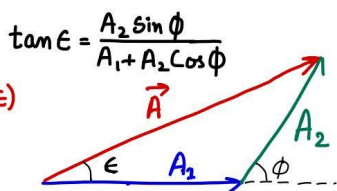


HOOK'S LAW $F = -kx$
 $x = A \sin(\omega t + \phi)$
 $v = A\omega \cos(\omega t + \phi)$
 $a = -\omega^2 x = -\frac{k}{m}x$
 $T = \frac{2\pi}{\omega} = 2\pi\sqrt{\frac{m}{k}}$

$K = \frac{1}{2}mv^2$
 $U = \frac{1}{2}kx^2$
 $E = K + U = \frac{1}{2}kA^2 = \frac{1}{2}m\omega^2 A^2$



$x_1 = A_1 \sin(\omega t)$
 $x_2 = A_2 \sin(\omega t + \phi)$
 $x = x_1 + x_2 = A \sin(\omega t + \epsilon)$
 $A = \sqrt{A_1^2 + A_2^2 + 2A_1A_2 \cos \phi}$



SERIES $\frac{1}{K_{eq}} = \frac{1}{K_1} + \frac{1}{K_2}$

PARALLEL $K_{eq} = K_1 + K_2$

PROPERTIES OF MATTER

YOUNG'S MODULUS $(Y) = \frac{F/A}{\Delta L/L}$

SHEAR MODULUS $(\eta) = \frac{F/A}{\tan \theta}$

BULK MODULUS $(B) = -V \frac{\Delta P}{\Delta V}$

COMPRESSIBILITY $(K) = \frac{1}{B} = -\frac{1}{V} \frac{\Delta V}{\Delta P}$

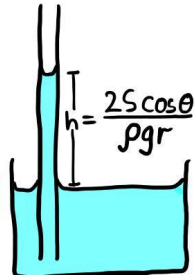
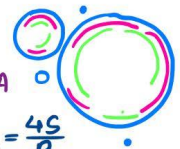
POISSON'S RATIO $(\sigma) = \frac{\text{LATERAL STRAIN}}{\text{LONGITUDINAL STRAIN}} = \frac{\Delta D/D}{\Delta L/L}$

ELASTIC ENERGY $(U) = \frac{1}{2} \text{STRESS} \times \text{STRAIN} \times \text{VOLUME}$

SURFACE TENSION $(S) = F/L$

SURFACE ENERGY $(U) = S \cdot \text{AREA}$

$P_{EXCESS} = \Delta P_{AIR} = \frac{2S}{R}$ $\Delta P_{SOAP} = \frac{4S}{R}$



$P_{HYDROSTATIC} = \rho gh$ $F_{BUOYANT} = \rho gV$

CONTINUITY $A_1 v_1 = A_2 v_2$

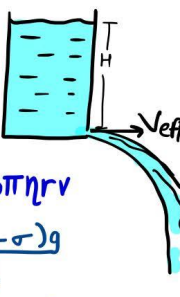


BERNOULLI'S $P + \rho gh + \frac{1}{2}\rho v^2 = \text{Const}$



$F_{VISCOUS} = -\eta A \frac{dv}{dx}$

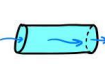
TORRICELLI'S $V_{EFFLUX} = \sqrt{2gh}$



STOKE'S LAW $F = 6\pi\eta r v$

$V_{TERMINAL} = \frac{2r^2(\rho - \sigma)g}{9\eta}$

POISEUILL'S EQN $\frac{\text{VOLUME FLOW}}{\Delta t} = \frac{\pi r^4 \Delta P}{8\eta L}$



WAVES

$\frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}$
 $y = A \sin(kx - \omega t)$
 $= A \sin\left[2\pi\left(\frac{x}{\lambda} - \frac{t}{T}\right)\right]$
 $T = \frac{1}{\nu} = \frac{2\pi}{\omega}$ $v = \nu\lambda$ **WAVE NUMBER** $(k) = \frac{2\pi}{\lambda}$

STANDING WAVES

$y_1 = A \sin(kx - \omega t)$ $y_2 = A \sin(kx + \omega t)$
 $y = 2A \cos kx \sin \omega t$ **Node** if $\cos$ is zero $\Rightarrow x = (n + \frac{1}{2})\lambda$

$L = n \cdot \frac{\lambda}{2}$ $v = \frac{n}{2L} \sqrt{\frac{T}{\mu}}$
SONOMETER

$L = (2n+1) \frac{\lambda}{4}$ $v = \frac{2n+1}{4L} \sqrt{\frac{T}{\mu}}$
OPEN $\Rightarrow$ ANTI NODE

SOUND WAVES

$S = S_0 \sin[\omega(t - x/v)]$ $v_{\text{solid}} = \sqrt{Y/\rho}$
 $P = P_0 \cos[\omega(t - x/v)]$ $v_{\text{liq}} = \sqrt{B/\rho}$
 $P_0 = \left[\frac{B\omega}{v}\right] s_0$ $v_{\text{gas}} = \sqrt{\gamma P/\rho}$
 $I = \frac{2\pi^2 B}{v} s_0^2 v^2 = \frac{P_0^2 v}{2B} = \frac{P_0^2}{2\rho v}$

STANDING LONGITUDINAL WAVES

$P_1 = P_0 \sin[\omega(t - x/v)]$ $P_2 = P_0 \sin[\omega(t + x/v)]$
 $P = P_1 + P_2 = 2P_0 \cos kx \sin \omega t$
CLOSED ORGAN PIPE
 $L = (2n+1) \frac{\lambda}{4}$ $v = (2n+1) \frac{v}{4L}$
OPEN ORGAN PIPE
 $L = n \frac{\lambda}{2}$ $v = n \frac{v}{2L}$

RESONANCE COLUMN

$L_1 + d = \frac{\lambda}{2}$ $L_2 + d = \frac{3\lambda}{2}$
 $v = 2(L_2 - L_1)\nu$

BEATS

(if $\omega_1 \approx \omega_2$)
 $P_1 = P_0 \sin \omega_1(t - x/v)$ $P_2 = P_0 \sin \omega_2(t - x/v)$
 $P = 2P_0 \cos \Delta\omega(t - x/v) \sin \omega(t - x/v)$
 $\omega = \frac{(\omega_1 + \omega_2)}{2}$ **Beats** $\rightarrow \Delta\omega = \omega_1 - \omega_2$

DOPPLER

$v = \frac{v + v_o}{v - v_s} v$

LIGHT WAVES

PLANE WAVES $E = E_0 \sin \omega(t - x/v)$; $I = I_0$

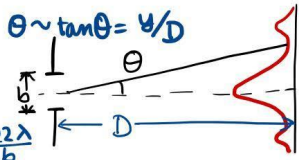
SPHERICAL WAVES $E = \frac{A E_0}{r} \sin \omega(t - r/v)$; $I = \frac{I_0}{r^2}$

DIFFRACTION

$\Delta x = b \sin \theta \approx b\theta$

Minima $b\theta = n\lambda$

Resolution $\sin \theta = \frac{1.22\lambda}{b}$



YOUNG'S DOUBLE SLIT EXPERIMENT

Path diff: $\Delta x = y \frac{d}{D}$ **Phase diff:** $\delta = \frac{2\pi}{\lambda} \Delta x$

CONSTRUCTIVE | DESTRUCTIVE

$\delta = 2n\pi$; $\Delta x = n\lambda$ $\delta = (2n+1)\pi$; $\Delta x = (n + \frac{1}{2})\lambda$

Intensity $I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta$ $I_{\text{max/min}} = (\sqrt{I_1} \pm \sqrt{I_2})^2$

Fringe Width $w = \frac{\lambda D}{d}$ **Optical Path** $\Delta x' = \mu \Delta x$

LAW of MALUS

$I = I_0 \cos^2 \theta$

INTERFERENCE THROUGH THIN FILM

$\Delta x = 2\mu d = \frac{n\lambda}{(2n+1)\lambda_2} \rightarrow$ **Constructive**
 $\rightarrow$ **destructive**

OPTICS

REFLECTION

(ii) $\angle i = \angle r$

(i) i, r & normal in same plane

$f = R/2$

$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$

Magnification $m = -\frac{v}{u}$

MICROSCOPE

Simple $m = D/f$

Compound

$m = \frac{v}{u} \frac{D}{f_e}$ **Resolving Pow** $R = \frac{1}{\Delta d} = \frac{2\mu \sin \theta}{\lambda}$

DISPERSION

Cauchy's $\mu = \mu_0 + A/\lambda^2$ $A > 0$

For small A & i

mean deviation $\delta_y = (\mu_y - 1)A$

Angular dispersion $\theta = (\mu_y - \mu_r)A$

Dispersive Power

$\omega = \frac{\mu_v - \mu_r}{\mu_y - 1} \approx \frac{\theta}{\delta_y}$

REFRACTION

$\mu = \frac{c}{v} = \frac{(\text{vacuum})}{(\text{medium})}$

SNELL'S LAW $\mu_1 \sin i = \mu_2 \sin r$

APPARENT DEPTH $d' = d/\mu$

TIR CRITICAL ANGLE

$\mu \sin \theta_c = 1$

PRISM

$\delta = i + i' - A$

$\mu = \frac{\sin \left(\frac{A + \delta_{\min}}{2}\right)}{\sin \left(\frac{A}{2}\right)}$

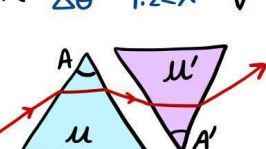
$\delta_{\min} = (\mu - 1)A$
 For small 'A'

TELESCOPE

$m = -f_o/f_e$

$L = f_o + f_e$

$R = \frac{1}{\Delta \theta} = \frac{1}{1.22\lambda}$



DISPERSION only

$(\mu_y - 1)A + (\mu'_y - 1)A' = 0$

DEVIATION only

$(\mu_v - \mu_r)A = (\mu'_v - \mu'_r)A'$

SPHERICAL SURFACE

$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$

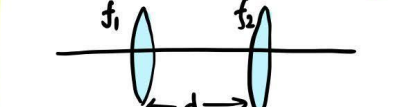
$m = \frac{\mu_1 v}{\mu_2 u}$

LENS MAKER'S $\frac{1}{f} = (\mu - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$

LENS FORMULA $\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$; $m = \frac{v}{u}$

POWER $P = 1/f$

THIN LENSES $\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2} - \frac{d}{f_1 f_2}$



PHYSICS

HEAT AND TEMP

$$F = 32 + \frac{9}{5}C$$

$$K = C + 273.16$$

$$\text{Ideal Gas} \rightarrow PV = nRT$$

$$\text{van der Waals}$$

$$(p + \frac{a}{V^2})(V - b) = nRT$$

$$L = L_0(1 + \alpha \Delta T)$$

$$A = A_0(1 + 2\alpha \Delta T)$$

$$V = V_0(1 + 3\alpha \Delta T)$$

$$\text{THERMAL STRESS}$$

$$\frac{F}{A} = Y \frac{\Delta L}{L}$$

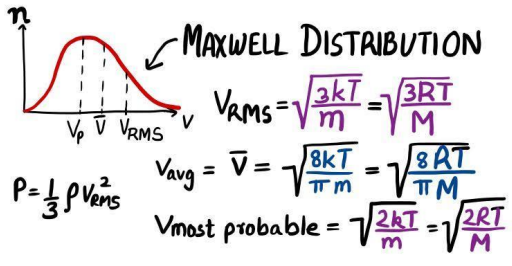
KINETIC THEORY

$$\text{EQUIPARTITION OF ENERGY}$$

$$K = \frac{1}{2}kT \text{ for each DoF}$$

$$K = \frac{F}{2}kT \text{ for } F \text{ Degrees of Freedom}$$

$$\text{Internal Energy } U = \frac{F}{2}nRT$$



$$F = 3 \text{ (monatomic)}; 5 \text{ (diatomic)}$$

SPECIFIC HEAT

$$\text{Specific heat } s = \frac{Q}{m\Delta T}$$

$$\text{Latent heat } L = Q/m$$

$$C_v = \frac{f}{2}R \quad C_p = C_v + R \quad r = C_p/C_v$$

$$C_v = \frac{n_1 C_{v1} + n_2 C_{v2}}{n_1 + n_2} \quad r = \frac{n_1 C_{p1} + n_2 C_{p2}}{n_1 C_{v1} + n_2 C_{v2}}$$

THERMODYNAMICS

$$\text{1st LAW } \Delta Q = \Delta U + W \quad W = \int p dV$$

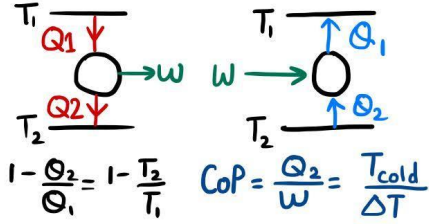
$$\text{ADIABATIC } W = \frac{p_1 V_1 - p_2 V_2}{\gamma - 1}$$

$$\text{ISOTHERMAL } W = nRT \ln\left(\frac{V_2}{V_1}\right)$$

$$\text{ISOBARIC } W = p(V_2 - V_1)$$

$$\text{ADIABATIC: } \Delta Q = 0; PV^\gamma = \text{Const}$$

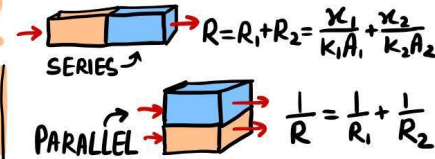
$$\text{IInd LAW ENTROPY } dS = \frac{dQ}{T}$$



HEAT TRANSFER

$$\text{CONDUCTION } \frac{\Delta Q}{\Delta t} = -KA \frac{\Delta T}{x}$$

$$\text{Thermal Resistance} = \frac{x}{KA}$$



$$\text{KIRCHHOFF'S LAW } \frac{\text{Emissive Power}}{\text{Absorptive Power}} = \frac{E_{body}}{a_{body}} = E_{blackbody}$$

$$\text{WIEN'S DISPLACEMENT } \lambda_m T = b$$

$$\text{STEFAN-BOLTZMANN } \Delta \theta / \Delta t = \sigma e A T^4$$

$$\text{NEWTON'S COOLING } \frac{dT}{dt} = -bA(T - T_0)$$

ELECTROSTATICS

$$\text{COULOMB'S LAW } F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

$$\vec{E} = \vec{F}/q = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

$$\text{POTENTIAL (V)} = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$

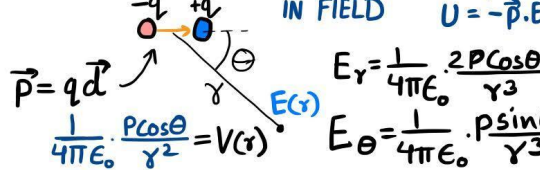
$$\text{PE (U)} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r} \quad \vec{E} = -\frac{dV}{dr}$$

$$\text{DIAPOLE MOMENT}$$

$$\text{DIAPOLE IN FIELD}$$

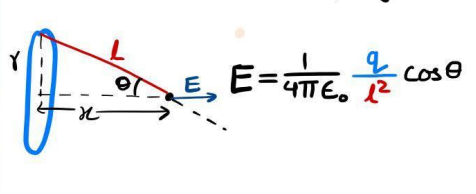
$$\vec{\tau} = \vec{p} \times \vec{E}$$

$$U = -\vec{p} \cdot \vec{E}$$

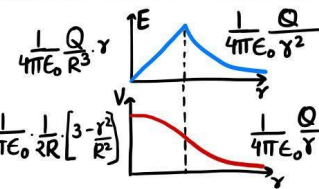


$$\text{GAUSS'S LAW}$$

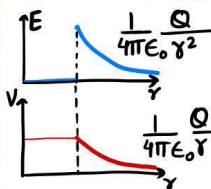
$$\phi = q_{in}/\epsilon_0 \quad \text{FLUX } \phi = \oint \vec{E} \cdot d\vec{s}$$



$$\text{UNIFORMLY CHARGED SPHERE}$$



$$\text{UNIFORM SHELL}$$



$$\text{LINE CHARGE } E = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\infty\text{-sheet } E = \frac{\sigma}{2\epsilon_0}$$

$$\vec{E} \text{ near } \text{CONDUCTING SURFACE } E = \frac{\sigma}{\epsilon_0}$$

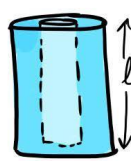
CAPACITORS

$$C = q/V \quad C = \epsilon_0 A/d$$



$$C = \frac{2\pi\epsilon_0 l}{\ln(r_2/r_1)}$$

$$C = 4\pi\epsilon_0 \frac{r_1 r_2}{r_2 - r_1}$$



$$\text{PARALLEL } C_{eq} = C_1 + C_2$$

$$\text{SERIES } \frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$\text{WITH DIELECTRIC } C = \frac{\epsilon_0 K A}{d}$$

$$\text{Force b/w plates} = \frac{Q^2}{2A\epsilon_0}$$

$$U = \frac{1}{2} CV^2 = \frac{Q^2}{2C} = \frac{1}{2} QV$$

CURRENT ELECTRICITY

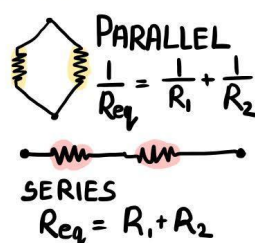
$$\text{DENSITY } j = I/A = \sigma E$$

$$V_{drift} = \frac{1}{2} \frac{eE\tau}{m} = \frac{i}{neA}$$

$$R_{wire} = \rho L/A \quad \rho = \frac{1}{\sigma}$$

$$R = R_0(1 + \alpha \Delta T)$$

$$\text{OHM'S LAW } V = iR$$

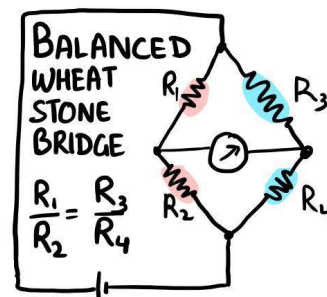


$$\text{KIRCHHOFF'S LAWS}$$

$$\text{* JUNCTION LAW } \sum I_i = 0$$

$$\text{* LOOP LAW } \sum \Delta V = 0$$

$$\text{POWER} = i^2 R = V^2/R = iV$$



GALVANOMETER

Ammeter
 $i_g G = (i - i_g) S$

Voltmeter
 $V_{AB} = i_g (R + G)$

CAPACITOR

Charging
 $q(t) = CV(1 - e^{-t/RC})$

Discharging
 $q(t) = q_0 e^{-(t/RC)}$

Time Constant $\tau = RC$

MAGNETISM

LORENTZ
 $\vec{F} = q\vec{v} \times \vec{B} + q\vec{E}$

$qvB = mv^2/r$
 $T = \frac{2\pi m}{qB}$

$\vec{F} = i\vec{L} \times \vec{B}$

MAGNETIC DIPOLE

$\vec{\mu} = i \text{Area} \vec{\hat{n}}$
 $\vec{\tau} = \vec{\mu} \times \vec{B}$
 $U = -\vec{\mu} \cdot \vec{B}$

HALL EFFECT

$V_H = \frac{Bi}{ned}$

PELTIER EFFECT

emf $e = \frac{\Delta H}{\Delta \theta}$

THOMSON EFFECT

emf $e = \frac{\Delta H}{\Delta \theta} = \sigma \Delta T$

FARADAY'S LAW OF ELECTROLYSIS

$m = Zit = \frac{1}{F} Fit$
 $E = \text{Chem equivalent}$
 $Z = \text{Electro Chem eq}$
 $F = 96485 \text{ C/g}$

SEEBACK EFFECT

$e = aT + \frac{1}{2}bT^2$
 $T_{\text{neutral}} = -a/b$
 $T_{\text{inversion}} = -2a/b$

BIOT-SAVART LAW

$d\vec{B} = \frac{\mu_0}{4\pi} i \frac{d\vec{L} \times \vec{r}}{r^3}$

STRAIGHT CONDUCTOR

$B_{\infty} = \frac{\mu_0 i}{2\pi d}$
 $B = \frac{\mu_0 i}{4\pi d} [\cos \theta_1 - \cos \theta_2]$

INFINITE WIRES

$\frac{dF}{dl} = \frac{\mu_0 i_1 i_2}{2\pi d}$

AXIS OF RING

$B_p = \frac{\mu_0 i r^2}{2(a^2 + r^2)^{3/2}}$

CENTER OF ARC

$B = \frac{\mu_0 i \theta}{4\pi r}$
 $B = \frac{\mu_0 i}{2r} (\text{ring})$

SOLENOID

$B = \mu_0 n i$
 $n = N/L$

TOROID

$B = \mu_0 n i$
 $n = N/2\pi r$

AMPERE'S LAW

$\oint \vec{B} \cdot d\vec{l} = \mu_0 I_{\text{enc}}$

BAR MAGNET

$B_1 = \frac{\mu_0}{4\pi} \frac{2M}{d^3}$
 $B_2 = \frac{\mu_0}{4\pi} \frac{M}{d^3}$

ANGLE OF DIP
 $B_h = B \cos \delta$
 $B_v = B \sin \delta$

TANGENT GALVANOMETER

$B_h \tan \theta = \mu_0 n i / 2r = k \tan \theta$

MOVING COIL GALVANOMETER

$n i A B = k \theta$
 $i = \frac{k}{nAB} \theta$

PERMEABILITY

$\vec{B} = \mu \vec{H}$

MAGNETOMETER

$T = 2\pi \sqrt{I/M B_h}$

ELECTROMAGNETIC INDUCTION

MAGNETIC FLUX $\Phi = \oint \vec{B} \cdot d\vec{s}$

FARADAY'S LAW $e = - \frac{d\Phi}{dt}$

LENZ'S LAW: Induced current produces $\vec{B}$ that opposes change in Φ

SELF INDUCTANCE

$\Phi = Li$
 $e = -L \frac{di}{dt}$

SOLENOID

$L = \mu_0 n^2 \pi r^2 l$

MUTUAL INDUCTANCE

$\Phi = Mi$
 $e = -M \frac{di}{dt}$

GROWTH

$i = \frac{V}{R} [1 - e^{-t/\tau}]$

DECAY

$i = i_0 e^{-t/\tau}$

Time Const. $\tau = L/R$
 ENERGY $U = \frac{1}{2} Li^2$

ENERGY DENSITY OF B-FIELD
 $u = \frac{U}{V} = \frac{B^2}{2\mu_0}$

ROTATING COIL $e = NAB\omega \sin \omega t$

TRANSFORMER

$\frac{N_1}{N_2} = \frac{e_1}{e_2}$
 $C = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$

ALTERNATING CURRENT

$i = i_0 \sin(\omega t + \phi)$
 $i_{\text{rms}} = i_0 / \sqrt{2}$
 POWER = $i_{\text{rms}}^2 R$

REACTANCE

CAPACITIVE $X_C = 1/\omega C$
 INDUCTIVE $X_L = \omega L$
 IMPEDANCE $Z = e_0/i_0$

RC-CIRCUIT

$\frac{1}{\omega C}$
 $\tan \phi = \frac{1}{\omega CR}$
 $Z = \sqrt{R^2 + X_C^2}$
 $X_C = \frac{1}{\omega C}$

LR-CIRCUIT

ωL
 $\tan \phi = \frac{\omega L}{R}$
 $Z = \sqrt{R^2 + X_L^2}$
 $X_L = \omega L$

LCR-CIRCUIT

$\tan \phi = \frac{X_C - X_L}{R}$
 $Z = \sqrt{R^2 + (X_C - X_L)^2}$
 $\nu_{\text{RESONANCE}} = \frac{1}{2\pi \sqrt{LC}}$
 $(X_C = X_L)$
 $P = e_{\text{rms}} i_{\text{rms}} \cos \phi$
 POWER FACTOR

MODERN PHYSICS

$E = h\nu = hc/\lambda$
 $p = h/\lambda = E/c$
 $E = mc^2$

Ejected photo-electron $K_{\text{max}} = h\nu - \phi$

THRESHOLD $\nu_0 = \phi/h$

STOPPING $V_0 = \frac{hc}{e} \left(\frac{1}{\lambda} - \frac{1}{\lambda_0} \right)$

de Broglie $\lambda = h/p$

BOHR'S ATOM

QUANTIZATION OF ANGULAR MOMENTUM
 $E_n = -\frac{mZ^2 e^4}{8\epsilon_0^2 h^2 n^2} = -\frac{13.6 Z^2}{n^2} \text{ eV}$
 $\gamma_n = \frac{E_n - E_m}{hc} = \frac{13.6 Z^2}{hc} \left(\frac{1}{m^2} - \frac{1}{n^2} \right)$
 $E_{\text{TRANSITION}} = 13.6 Z^2 \left(\frac{1}{n^2} - \frac{1}{m^2} \right) \text{ eV}$

HEISENBERG

$\Delta x \Delta p \geq h/2\pi$
 $\Delta E \Delta t \geq h/2\pi$

MOSLEY'S LAW

$\sqrt{\nu} = a(Z - b)$

X-RAY DIFFRACTION

$2d \sin \theta = n\lambda$

NUCLEUS

$R = R_0 A^{1/3}$
 $R_0 = 1.1 \times 10^{-15} \text{ m}$

RADIOACTIVE DECAY

$\frac{dN}{dt} = -\lambda N$
 $N = N_0 e^{-\lambda t}$
 HALF LIFE $t_{1/2} = 0.693/\lambda$
 Avg LIFE $t_{\text{avg}} = 1/\lambda$

Mass DEFECT

$\Delta m = [Zm_p + (A-Z)m_n] - M$
 BINDING $E = \Delta m \cdot c^2$

Q-VALUE $Q = U_i - U_f$

X-Ray SPE^M

SEMICONDUCTORS

HALF WAVE RECTIFIER

FULL WAVE RECTIFIER

TRIODE VALVE

TRIODE

Plate Resistance $r_p = \frac{\Delta V_p}{\Delta i_p} \bigg|_{\Delta V_g = 0}$

Trans-conductance $g_m = \frac{\Delta i_p}{\Delta V_g} \bigg|_{\Delta V_p = 0}$

Amplification $\mu = \frac{\Delta V_p}{\Delta V_g} \bigg|_{\Delta i_p = 0}$

$\mu = r_p \times g_m$

TRANSISTOR

$I_e = I_b + I_c$

$\alpha = \frac{I_c}{I_e}$
 $\beta = \frac{I_c}{I_b}$
 $\beta = \frac{\alpha}{1-\alpha}$

Transconductance $g_m = \frac{\Delta I_c}{\Delta V_{be}}$

LOGIC GATES

AND, OR, NOT, NAND, NOR, XOR

Truth Table for AND, OR, NOT, NAND, NOR, XOR

Truth Table for AND, OR, NOT, NAND, NOR, XOR

Truth Table for AND, OR, NOT, NAND, NOR, XOR

Truth Table for AND, OR, NOT, NAND, NOR, XOR

NOW, YOU'RE ONE STEP CLOSER TO YOUR GOAL